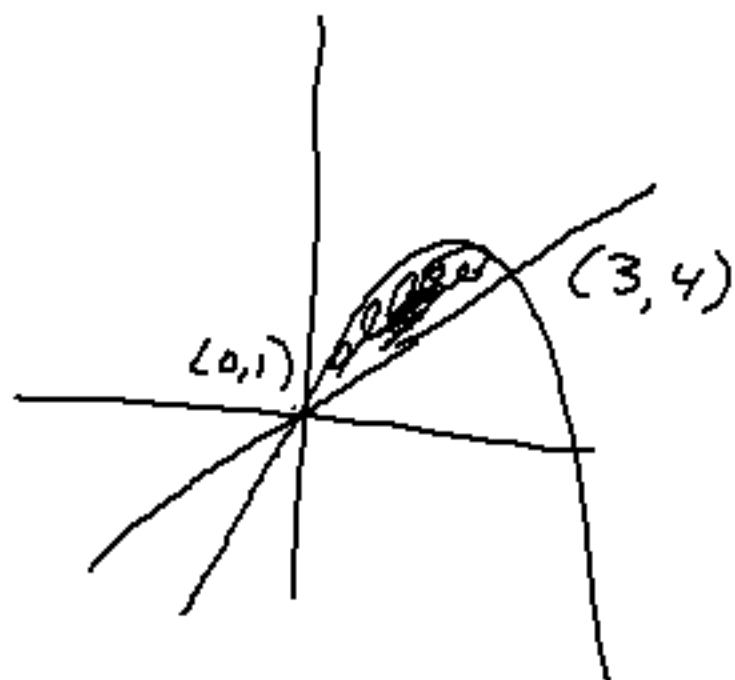


p 452

(20) $f(x) = -x^2 + 4x + 1$

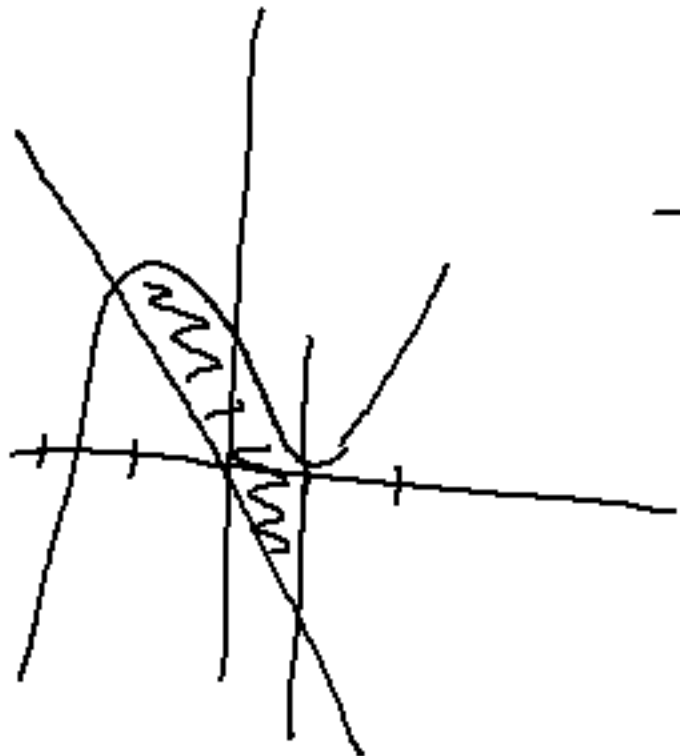
$g(x) = x + 1$



$$\int_0^3 (-x^2 + 4x + 1 - (x + 1)) dx$$
$$= 4.5$$

34 $f(x) = x^3 - 2x + 1$
 $g(x) = -2x$

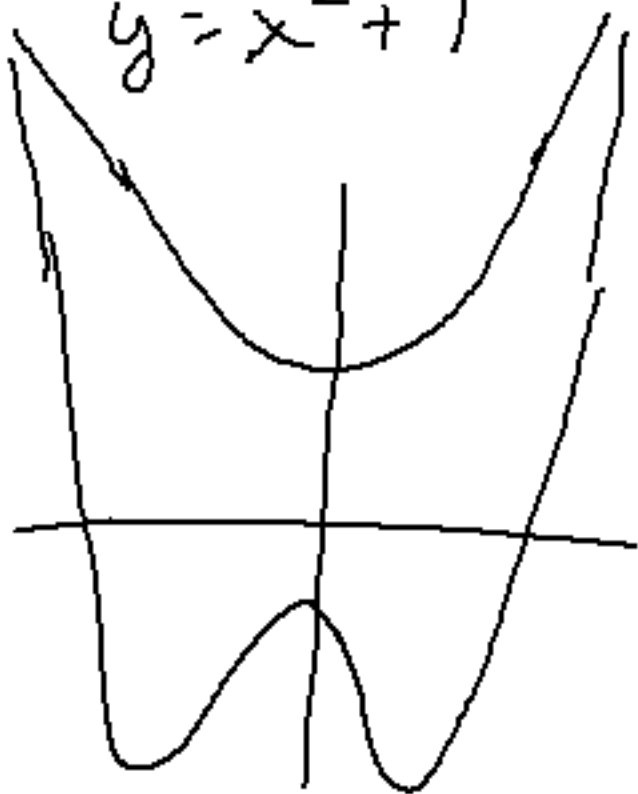
$x = 1$



$$\int_{-1}^1 (x^3 - 2x + 1 - (-2x)) dx$$
$$= 2$$

ex) $y = x^4 - 5x^2 - 1$

$y = x^2 + 1$



$$\int_{-2.51329}^{2.5132896} (x^2 + 1 - (x^4 - 5x^2 - 1)) dx$$

$$= 33.443$$

$$\text{ex) } y = x^3 + x^2 - 5$$

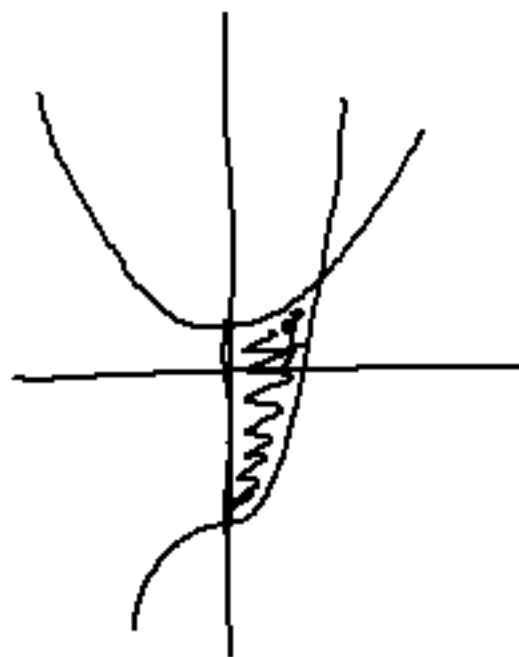
$$y = \frac{1}{2}x^2 + 1$$

$$x = 0$$

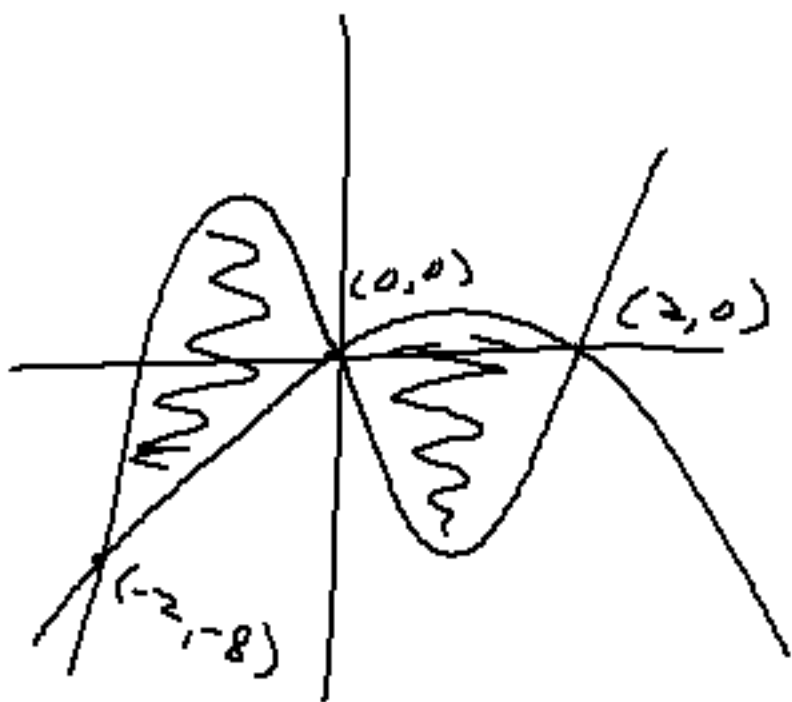
$$1.6648129$$

$$\int_0^{1.6648129} \left(\frac{1}{2}x^2 + 1 - (x^3 + x^2 - 5) \right) dx$$

$$= 7.299$$



p 449 ex 4.



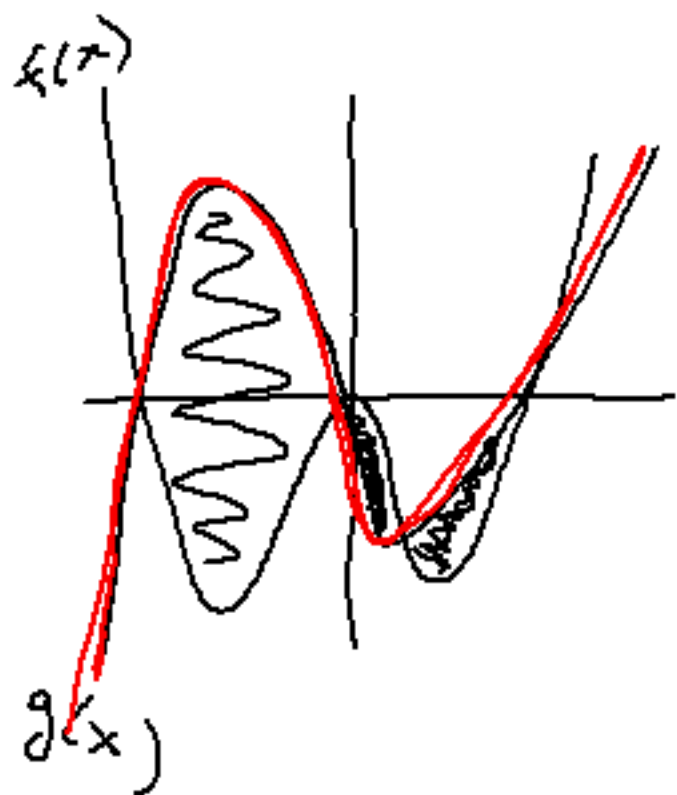
$$\int_{-2}^0 (3x^3 - x^2 - 10x - (-x^2 + 2x)) dx$$
$$+ \int_0^2 (-x^2 + 2x - (3x^3 - x^2 - 10x)) dx$$

$$= 12 + 12 = 24$$

p 452 #38

$$f(x) = x^4 - 4x^2$$

$$g(x) = x^3 - 4x$$



$$\int_{-2}^0 g(x) - f(x) dx = 8.26666$$

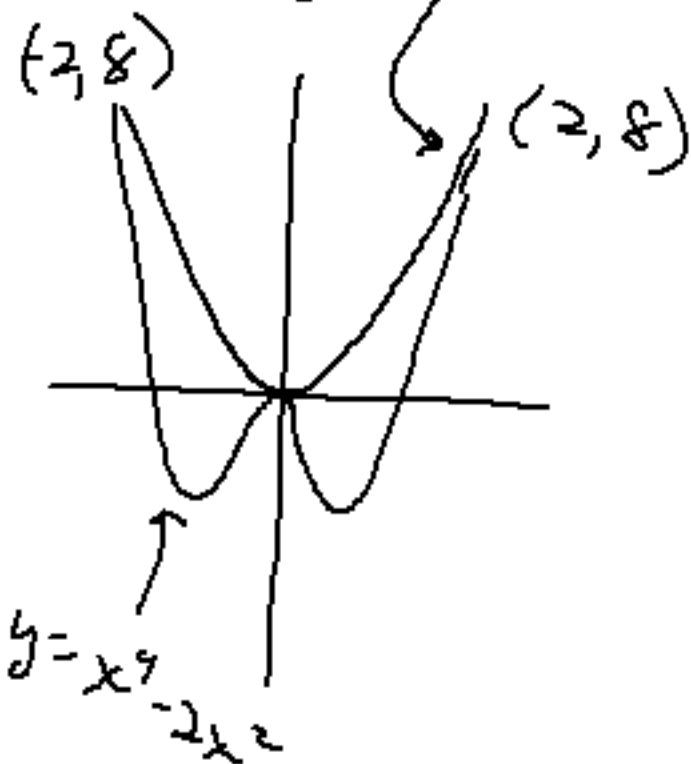
$$\int_0^1 f(x) - g(x) dx = .616666$$

$$\int_{-1}^2 g(x) - f(x) dx = .883333$$
$$= 9.767$$

#36

$$y = x^4 - 2x^2$$

$$y = 2x^2$$



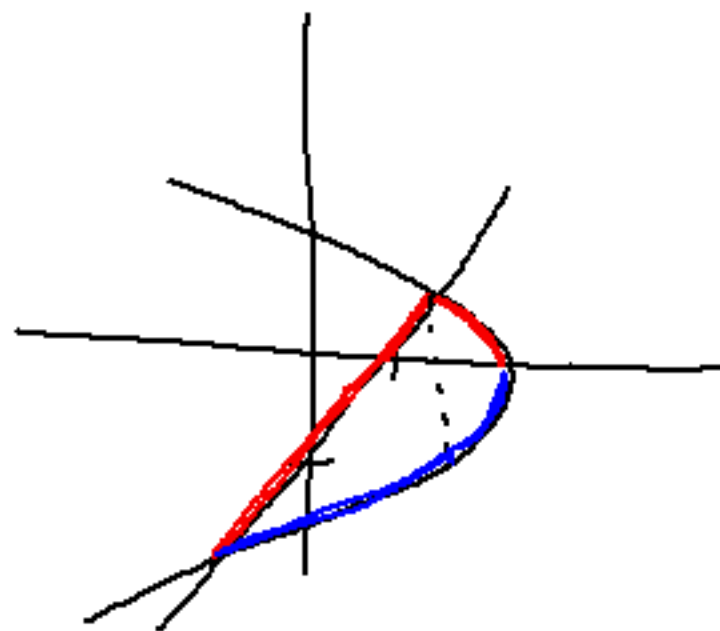
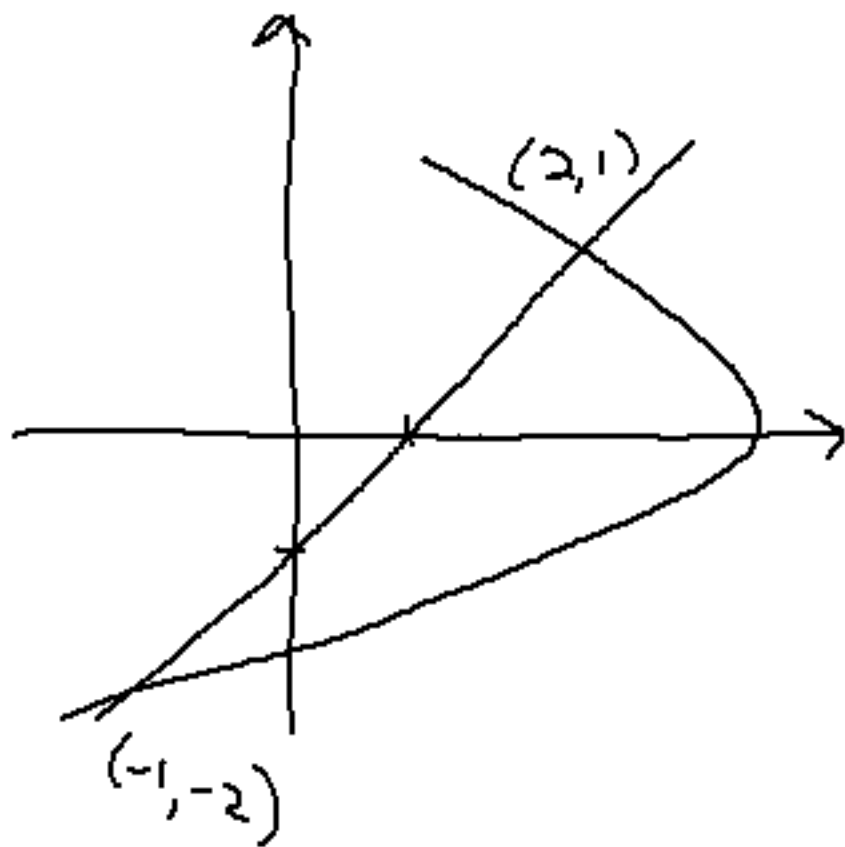
$$\int_{-2}^2 2x^2 - (x^4 - 2x^2) dx$$
$$= 8.533$$

450 ex 5

$$x = 3 - y^2$$

$$x = y + 1$$

$$\int_{-2}^1 (3 - y^2 - (y + 1)) dy$$
$$= 4.5$$

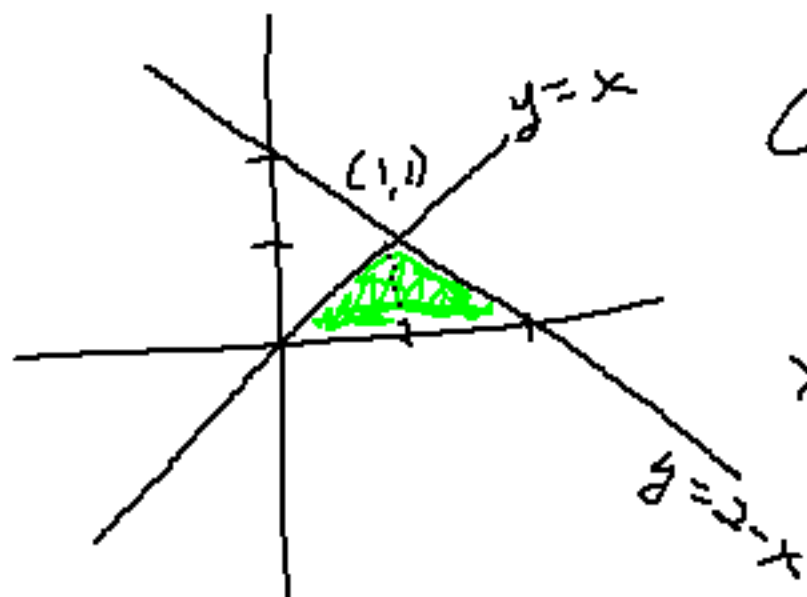


p 452 # 23

$$y = x$$

$$y = 2 - x$$

$$y = 0$$



$$\int_0^1 x - 0 \, dx$$
$$+ \int_1^2 2 - x - 0 \, dx$$

$$= .5 + .5 = 1$$

OR

$$x = y$$

$$x = 2 - y$$

$$\int_0^1 2 - y - y \, dy$$

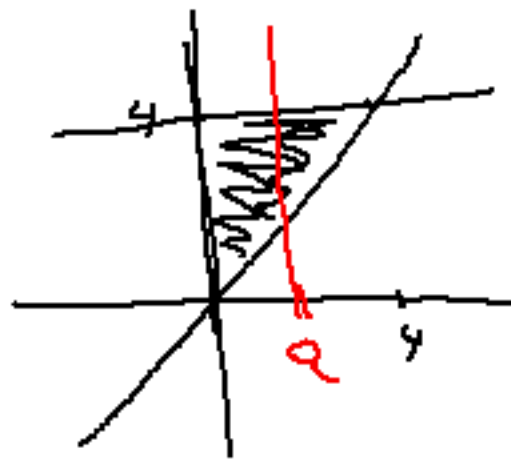
$$= 1$$

p 454
77

$$y = x$$

$$y = 4$$

$$x = 0$$



$$\int_0^a 4 - x \, dx = \int_a^4 4 - x \, dx$$

$$\left[4x - \frac{1}{2}x^2 \right]_0^a = \left[4x - \frac{1}{2}x^2 \right]_a^4$$

$$4a - \frac{1}{2}a^2 - 0 = 8 - \left(4a - \frac{1}{2}a^2 \right)$$

$$4a - \frac{1}{2}a^2 = 8 - 4a + \frac{1}{2}a^2$$

$$0 = a^2 - 8a + 8$$

$$a = 1.172$$

p 452

6, 136, 25, 31, 37, 56