

Review the concepts and sample problems that follow. Both will be helpful in completing the packet.

When simplifying expressions involving positive and negative numbers:

I. Rewrite expression without double notation (2 signs in front of a number).

Example:

a) $3+(+2)$
 $3+2$

b) $3+(-2)$
 $3-2$

c) $3-(-2)$
 $3+2$

d) $3-(+2)$
 $3-2$

II. Then use the following rules to add or subtract the terms.

1) Same signs – keep the sign and add the numbers

2) Different signs- take the sign of the larger number and subtract the numbers.

Sample Problems:

1) $7+(-10)$
 $7-10$
 -3

2) $5-(-4)$
 $5+4$
 9

3) $-6-(-9)$
 $-6+9$
 3

4) $-2-2$
 -4

5) $-8+12$
 4

6) $4-(+6)$
 $4-6$
 -2

When multiplying or dividing positive and negative numbers:
(2 numbers at a time).

1) Same signs – positive

2) Different signs – negative

Sample Problems:

1) $(-4)(-3)$
 12

2) $\frac{-6}{2}$
 -3

3) $(-2)(-3)(-4)$
 -24

4) $\frac{-20}{-4}$
 5

Remember to combine “like terms” when simplifying expressions involving addition or subtraction:

$$\begin{array}{l}
 2x + 3 + 4x - 5 \\
 \underbrace{2x + 4x} + \underbrace{3 - 5} \quad \text{(Rearrange terms mentally)} \\
 6x - 2 \quad \text{(Combine)}
 \end{array}$$

Use order of operations when simplifying:

$$\begin{array}{l}
 (4 - 8) - (-20 + 25) \\
 (-4) - (5) \\
 -4 - 5 \\
 -9
 \end{array}$$

Use the distributive property when appropriate:

$$\begin{array}{ll}
 \begin{array}{l}
 \overset{\curvearrowright}{4(x - 2)} \\
 4(x) - 4(2) \\
 4x - 8
 \end{array} &
 \begin{array}{l}
 \overset{\curvearrowright}{2(a - 3b)} \\
 2(a) + 2(-3b) \\
 2a - 6b
 \end{array}
 \end{array}$$

To evaluate expressions, replace the variables with the numerical values given and simplify.

Sample Problems:

Evaluate if: $a = -2$ and $b = -3$

1) $a - b$

$$(-2) - (-3)$$

$$-2 + 3$$

$$1$$

2) $-3a + b$

$$-3(-2) + (-3)$$

$$6 - 3$$

$$3$$

3) $\frac{4 + ab}{a - b}$

$$\frac{4 + (-2)(-3)}{-2 - (-3)}$$

$$10$$

4) $-2ab$

$$-2(-2)(-3)$$

$$-12$$

When Solving Equations:

- 1) Simplify each side of the equation as needed.
- 2) Use inverse operations to “undo” the operations in the equations.

(Show all work. Do not solve mentally and do not use a calculator.)

Sample Problems:

$$\begin{aligned} 1) \quad x - (-3) &= 10 \\ x + 3 &= 10 \\ -3 &\quad -3 \\ x &= 7 \end{aligned}$$

Rewrite without double notation
Subtract 3 from both sides and simplify

$$\begin{aligned} 2) \quad n + (-5) &= -20 \\ n - 5 &= -20 \\ +5 &\quad +5 \\ n &= -15 \end{aligned}$$

Rewrite without double notation
Add 5 to both sides and simplify

$$\begin{aligned} 3) \quad -2n + 4 &= -8 \\ -4 &\quad -4 \\ \underline{-2n} &= \underline{-12} \\ -2 &\quad -2 \\ n &= 6 \end{aligned}$$

Subtract 4 from both sides
Divide both sides by -2 and simplify

$$\begin{aligned} 4) \quad \frac{n}{-3} + 9 &= 6 \\ -9 &\quad -9 \\ (-3) \left(\frac{n}{-3} \right) &= (-3)(-3) \\ n &= 9 \end{aligned}$$

Subtract 9 from both sides
Multiply both sides by -3 and simplify

$$\begin{aligned} 5) \quad 4x - x - 5 &= 7 \\ 3x - 5 &= 7 \\ +5 &\quad +5 \\ \underline{3x} &= \underline{12} \\ 3 &\quad 3 \\ x &= 4 \end{aligned}$$

Simplify left side of equation
Add 5 to both sides
Divide both sides by 3 and simplify

PRACTICE PROBLEMS

Simplify:

- 1) $6 - 16$
- 2) $-6 + 9$
- 3) $6 + (-9)$
- 4) $-4 - 4$
- 5) $-4 - (-4)$
- 6) $7 - (-5)$
- 7) $-8 + (-3)$
- 8) $36 + (+2)$
- 9) $-8 - (+1)$
- 10) $-2 + 5 - 4$
- 11) $-5 + (-3) + 6$
- 12) $2 + 5y + 8$
- 13) $3 + 4 + 2w$
- 14) $a + 2 + b + 5$
- 15) $4 + 6xy + 2 = 3xy$
- 16) $-8 - 2x + 2$
- 17) $-5a - 3a - 2 - 1$
- 18) $3y - (-7) - y + 6$
- 19) $-[6 + (-1)] + (-c)$
- 20) $50 - (45 - 5)$
- 21) $-3 + (-9) + 7$
- 22) $(2 - 7) - (-12 + 15)$
- 23) $18 - 10 \div (3 + 2)$
- 24) $3[20 - (5 + 3)]$
- 25) $(125 - 150) - (20 - 45)$
- 26) $2y - 5 - 5y + 3$
- 27) $11a - 11 - 5a + 5$
- 28) $3(20a)$
- 29) $(5x)(-6y)$
- 30) $(6x)(y)(4z)$
- 31) $(-2)(-3)$
- 32) $8(-4)$
- 33) $(-2)(5)(-8)$
- 34) $5(-2)(-1)(-3)$
- 35) $5(-2) - (-1)$
- 36) $(-6a)(-5b)$
- 37) $3y + (-7y)$
- 38) $2(x + 3)$
- 39) $5(n - 1)$
- 40) $5(2x + 4)$
- 41) $3(2x - 3y)$
- 42) $-6(x - 2y)$
- 43) $2 - 5(x + 2)$
- 44) $3x - 5(x - 1)$
- 45) $4 + 3(x - 6) - 5$
- 46) $-4[3(x - 6) + 2] - (-2)$
- 47) $(3x + 10) - 2(x + 10)$
- 48) $(x + 3) + (x + 3)$
- 49) $(-16x - 2y) + (-3x + 7y)$
- 50) $(-9y + 7y + 7) - (6x - 2y - 7)$

Practice Problems:

Use inverse operations to solve each equation. Show all work. (DO NOT SOLVE MENTALLY).

1. $d - 9 = 11$

2) $a + 14 = 5$

3) $n - (-4) = 12$

4) $x - 27 = -54$

5) $7 - y = 11$

6) $5x = -20$

7) $n + (-4) = -10$

8) $-10y = 5$

9) $\frac{c}{6} = -4$

10) $-20 = \frac{n}{5}$

11) $\frac{-x}{3} = 15$

12) $\frac{2n}{3} = 4$

13) $\frac{-5}{8}n = -10$

14) $\frac{-1}{3}y = 7$

15) $x + 5 + (6 - 2) = 10$

16) $2a + 3a = 20$

17) $-3n + 9n = 24$

18) $y - 4y = -18$

19) $2(x - 3) = 10$

20) $3y + 2 = 17$

21) $2x - 3 = 15$

22) $\frac{1}{3}x + 5 = 7$

23) $3(a - 1) + 5 = 32$

24) $\frac{x - 1}{2} = 5$

25) $-3 = 7(h - 2) + 11$

Evaluate each expression if: $x = -2$, $y = 5$ and $z = -3$

1) $3xy$

2) $3x^2$

3) $-3x^2$

4) $-3x^2z$

5) $x - y - z$

6) $y + z + 9 - 2$

7) $-1 + (-x) + (-y)$

8) $-(-x) - (-y)$

9) $2x - 3z$

10) $\frac{2x - y}{z}$

11) $2x + 5$

12) $2(x + 5)$

Simplify. When appropriate, leave all answers as improper fractions in simplest form. NO CALCULATOR!!

To be successful in honors math, all students must be able to find the answer using mental math or paper/pencil.

1. $\frac{36}{12}$

2. $\frac{33}{9}$

3. $\frac{500}{5000}$

4. $\frac{3}{12}$

5. $\frac{24}{7}$

6. $\frac{15}{60}$

7. $4\frac{1}{6} + 3\frac{5}{6}$

8. $\frac{7}{8} + \frac{2}{8} + \frac{1}{8}$

9. $\frac{2}{3} + \frac{3}{4}$

10. $\frac{2}{3} + \frac{4}{5}$

11. $\frac{8}{12} - \frac{2}{12}$

12. $\frac{3}{4} - \frac{5}{8}$

13. $9\frac{1}{4} - \frac{1}{2}$

14. $6\frac{4}{5} - 5\frac{4}{5}$

15. $\frac{5}{2} \times \frac{6}{4}$

16. $2\frac{1}{3} \times \frac{6}{5}$

17. $\frac{2}{5} \times \frac{3}{16}$

18. $\frac{3}{8} \times 12$

19. $100 \div \frac{1}{3}$

20. $\frac{2}{5} \div \frac{7}{5}$

21. $2\frac{1}{5} \div 5$

22. $3 + 1\frac{1}{2}$